



Virtual Memory

Amir H. Payberah
payberah@kth.se
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Motivation

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- ▶ Only **part of the program** needs to be in memory for **execution**.

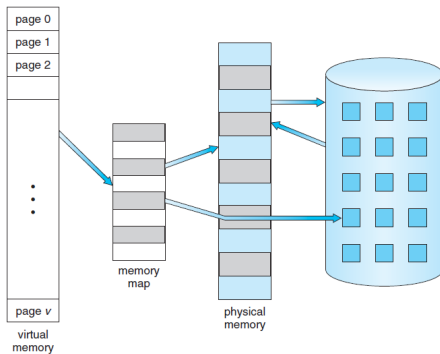


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- ▶ But, **entire program rarely used** (e.g., unusual routines, large data structures).
- ▶ Only **part of the program** needs to be in memory for **execution**.
- ▶ **More programs** running **concurrently**.

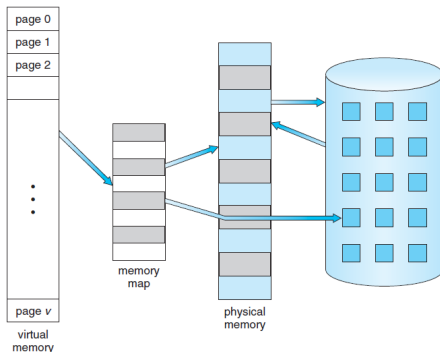
Virtual Memory

- Separation of user logical memory from physical memory.



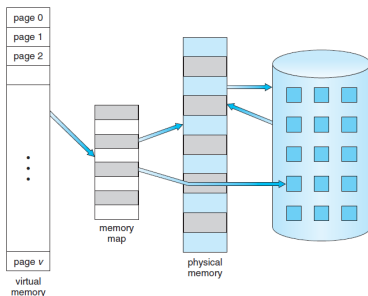
Virtual Memory

- ▶ Separation of user logical memory from physical memory.
- ▶ Logical address space can be much larger than physical address space.



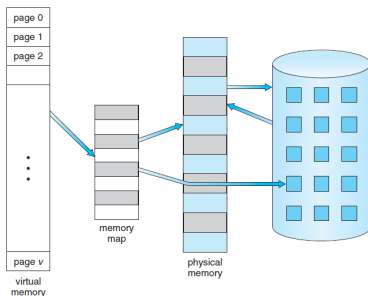
Virtual Address Space (1/2)

- ▶ **Virtual address space:** logical view of how process is stored in memory.



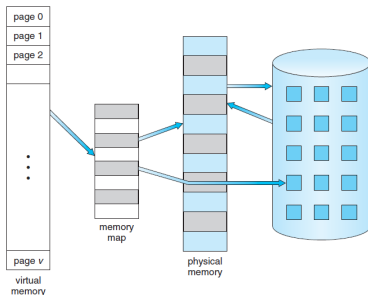
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- ▶ Meanwhile, **physical memory** organized in page **frames**.



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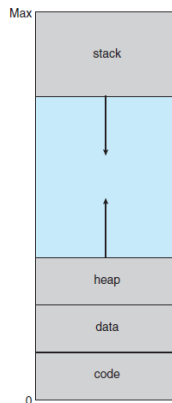
- ▶ **Virtual address space**: logical view of how process is stored in memory.
- ▶ Meanwhile, **physical memory** organized in page **frames**.
- ▶ **MMU** must map logical to physical.





Virtual Address Space (2/2)

- ▶ The **hole** between **heap** and **stack** is part of the **virtual address space**, but will require actual physical pages only if the heap or stack **grows**.

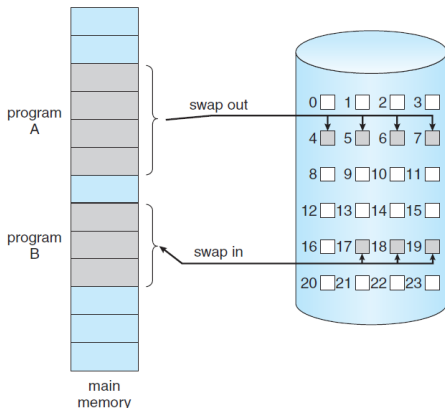




Demand Paging

Demand-Paging

- ▶ Demand-paging: bring a page into memory only when it is needed.
- ▶ lazy swapper.



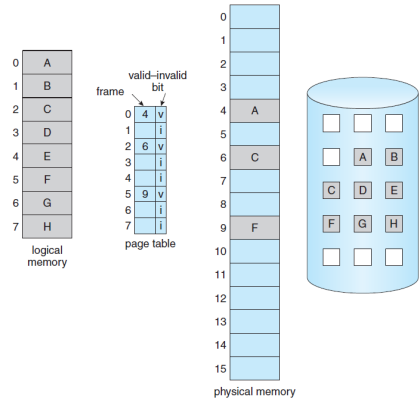


Basic Concepts

- ▶ The **pager** guesses **which pages** will be used again **before swapping out**.

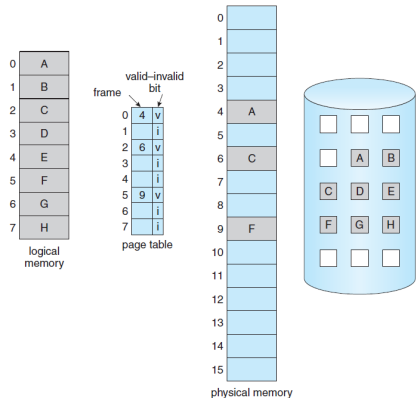
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Basic Concepts

- ▶ The **pager** guesses **which pages** will be used again **before swapping out**.
- ▶ **Valid-invalid bit**: **distinguish** between the pages in **memory** and on **disk**.
 v: memory resident
 i: not in memory



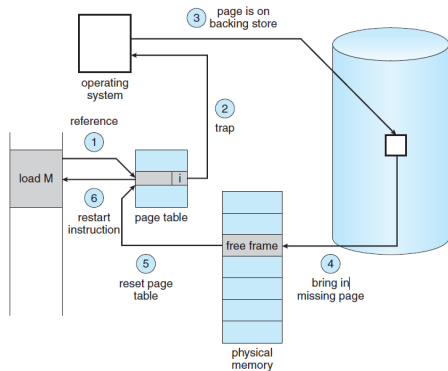


Page Fault

- ▶ Access to a page marked **invalid** causes a **page fault**.
- ▶ Causing a trap to the OS: brings the **desired page into memory**.

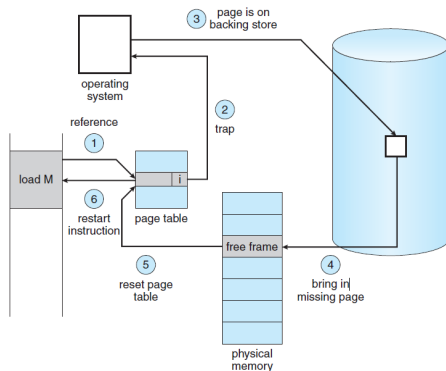
Handling Page Fault (1/6)

- ▶ Check an **internal table** for the process to determine whether the reference was a **valid** or an **invalid** memory access.



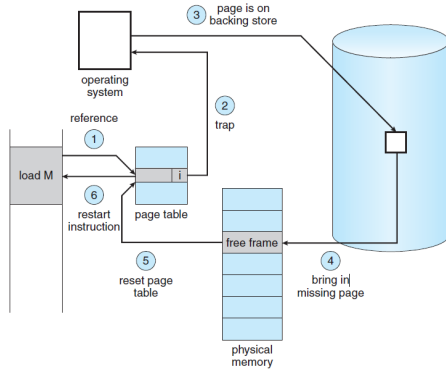
Handling Page Fault (2/6)

- ▶ If the reference was **invalid**, we **terminate** the process.



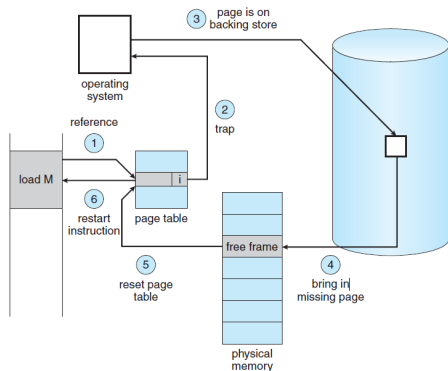
Handling Page Fault (2/6)

- ▶ If the reference was **invalid**, we **terminate** the process.
- ▶ If it was **valid** but we have not yet brought in that page, we now **page it in**.



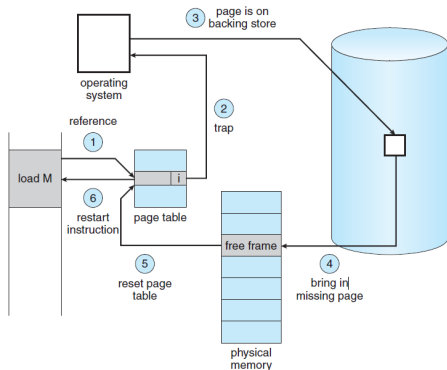
Handling Page Fault (3/6)

- ▶ We find a free frame.



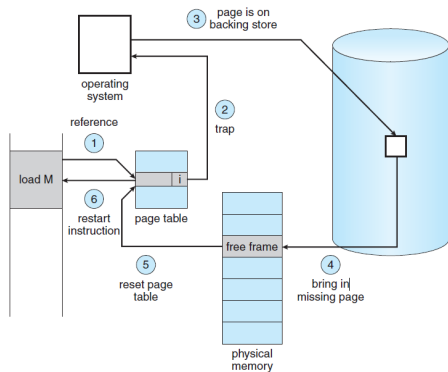
Handling Page Fault (4/6)

- ▶ We schedule a disk operation to **read the desired page** into the newly allocated frame.



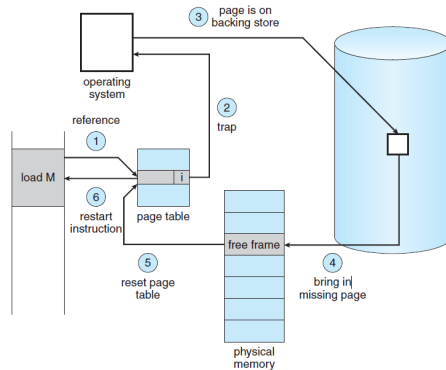
Handling Page Fault (5/6)

- ▶ When the disk read is complete, we **modify** the **internal table** kept with the process and the page table to indicate that the page is now in memory.



Handling Page Fault (6/6)

- ▶ We restart the instruction that was interrupted by the trap.



Page Replacement



What Happens if There is no Free Frame?

- ▶ Assume, we had 40 frames in physical memory.
- ▶ And, we run 6 processes, each of which is 10 pages in size, but actually uses only 5 pages.



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- ▶ Increasing the degree of multiprogramming: over-allocating memory



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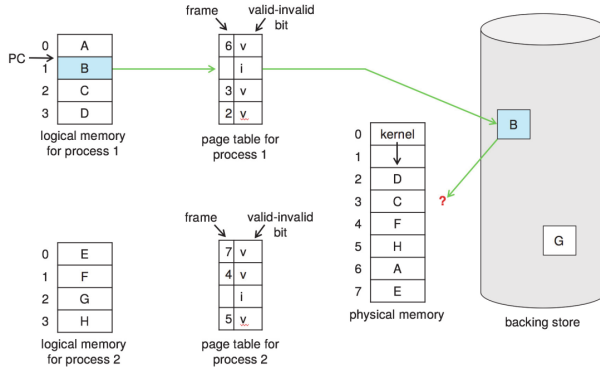
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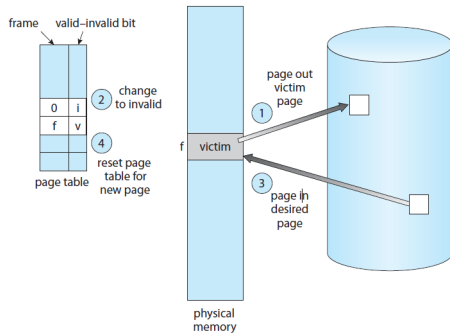
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- ▶ **Need for page replacement**

Need For Page Replacement



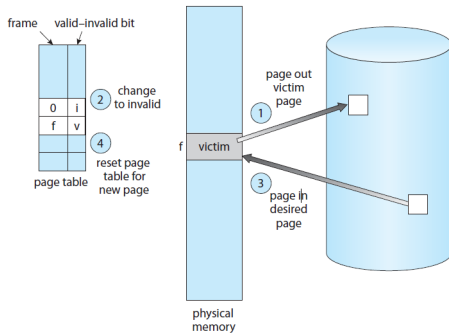
Page Replacement (1/4)

- Find the location of the desired page on disk.



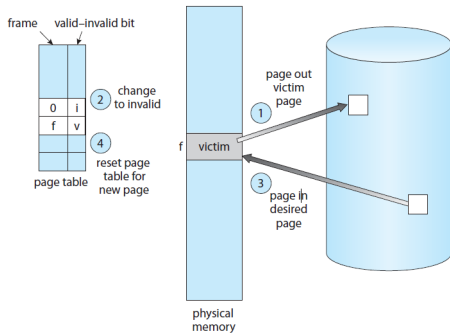
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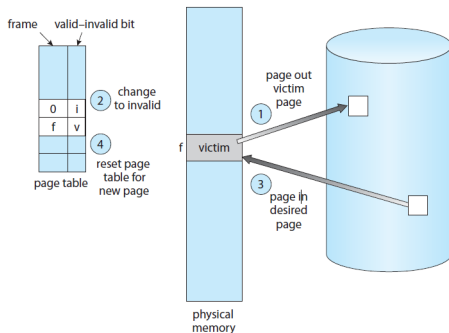
Page Replacement (2/4)

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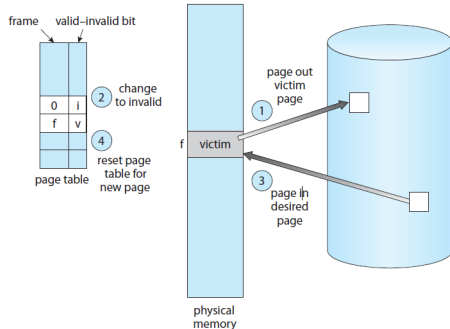
Page Replacement (2/4)

- ▶ Find a **free frame**.
 - If there is a **free frame**, use it.
 - If there is **no free frame**, use a **page replacement algorithm** to select a **victim frame**: **write** victim frame to disk if **dirty**.



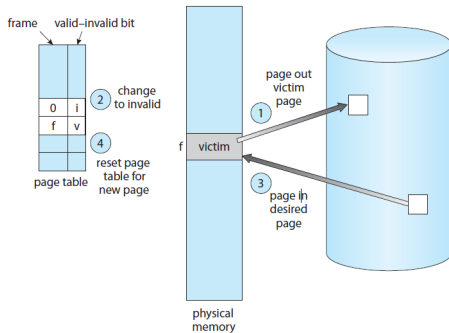
Page Replacement (3/4)

- ▶ Bring the desired page into the (newly) free frame; **update** the page and frame tables

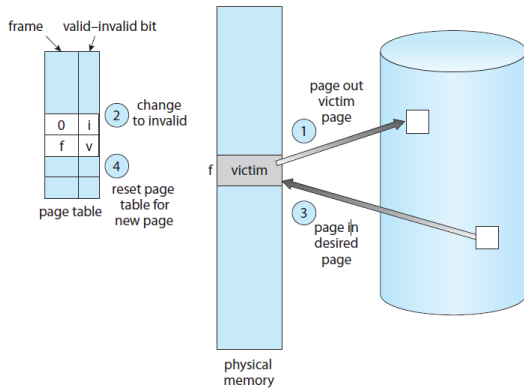


Page Replacement (4/4)

- ▶ Continue the process by **restarting the instruction** that caused the trap.



Dirty Bit



- ▶ Use **modify (dirty) bit** to **reduce overhead** of page transfers - only **modified pages** are written to disk.



Page Replacement Algorithms



Evaluate Page Replacement Algorithms

- ▶ **Reference string** is a sequence of **page numbers**.



Evaluate Page Replacement Algorithms

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- ▶ Assume a **reference string** could be
7, 0, 1, 2, 0, 3, 0, 4, 2, 3, 0, 3, 0, 3, 2, 1, 2, 0, 1, 7, 0, 1



Evaluate Page Replacement Algorithms

- ▶ **Reference string** is a sequence of **page numbers**.
- ▶ Assume a **reference string** could be
7, 0, 1, 2, 0, 3, 0, 4, 2, 3, 0, 3, 0, 3, 2, 1, 2, 0, 1, 7, 0, 1
- ▶ **Evaluate algorithm** by running it on a **reference string** and computing the **number of page faults** on that string.



Page Replacement Algorithms

- ▶ First-In-First-Out (FIFO)
- ▶ Optimal
- ▶ Least Recently Used (LRU)
- ▶ LRU-Approximation
- ▶ Counting-Based

FIFO Page Replacement



FIFO Page Replacement

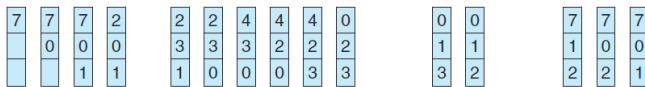
- ▶ Reference string: 7,0,1,2,0,3,0,4,2,3,0,3,0,3,2,1,2,0,1,7,0,1

FIFO Page Replacement

- ▶ Reference string: 7,0,1,2,0,3,0,4,2,3,0,3,2,1,2,0,1,7,0,1
- ▶ 3 frames (3 pages can be in memory at a time per process)

reference string

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page frames

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page frames

- ▶ 15 page faults



Optimal Page Replacement



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Optimal Page Replacement

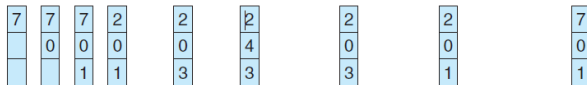
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Optimal Page Replacement

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7	7	7	2		2		2		2		2		2				7		
	0	0	0		0		4		0		0		0				0		
		1	1		3		3		3		1						1		

page frames

- ▶ Used for measuring **how well your algorithm performs**.



LRU Page Replacement



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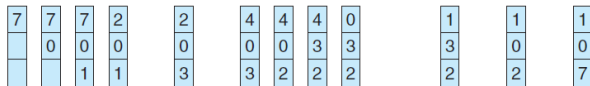
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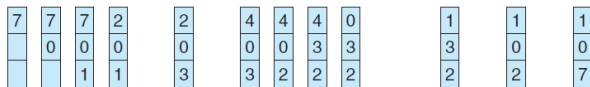
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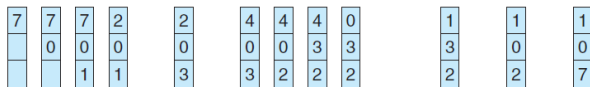
- ▶ **12 faults: better than FIFO but worse than OPT**

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page frames

- ▶ **12 faults: better than FIFO but worse than OPT**
- ▶ Generally good algorithm and frequently used



LRU Implementation (1/2)

- ▶ Counter implementation



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- ▶ Every page entry has a **counter**; every time page is referenced through this entry, copy the **clock into the counter**.



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- ▶ When a page needs to be changed, look at the counters to find **smallest value**.



LRU Implementation (1/2)

- ▶ Counter implementation
- ▶ Every page entry has a counter; every time page is referenced through this entry, copy the clock into the counter.
- ▶ When a page needs to be changed, look at the counters to find smallest value.
- ▶ Search through table needed.



LRU Implementation (2/2)

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- ▶ Page referenced: move it to the top

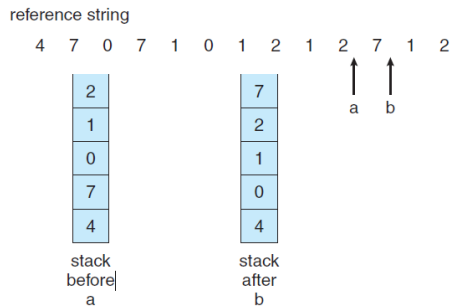


LRU Implementation (2/2)

- ▶ Stack implementation
- ▶ Keep a stack of page numbers in a double link form.
- ▶ Page referenced: move it to the top
- ▶ No search for replacement.

Stack Implementation

- Use of a stack to record **most recent page references**.



LRU-Approximation Page Replacement



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- ▶ LRU needs **special hardware** and still **slow**
- ▶ Improvements: **LRU-Approximation**



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 - Second-chance algorithm



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Reference Bit

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- ▶ When page is referenced, bit set to 1
- ▶ Replace any with reference bit = 0 (if one exists)
- ▶ We do not know the order



Second-Chance Algorithm (1/2)

- ▶ Generally **FIFO**, plus hardware-provided **reference bit**



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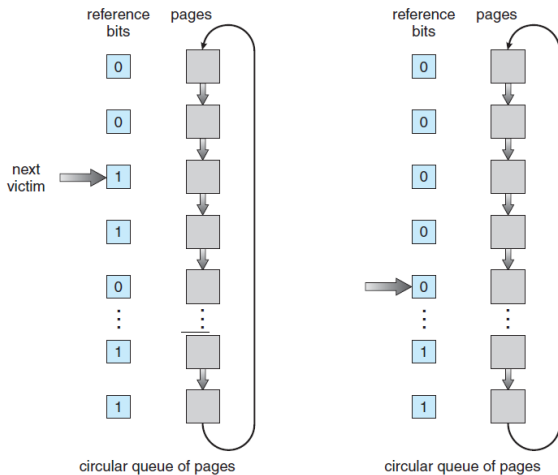
- ▶ Generally **FIFO**, plus hardware-provided **reference bit**
- ▶ If page to be replaced has
 - Reference bit = 0 → **replace it**



Second-Chance Algorithm (1/2)

- ▶ Generally **FIFO**, plus hardware-provided **reference bit**
- ▶ If page to be replaced has
 - Reference bit = **0** → **replace it**
 - Reference bit = **1** then, set reference bit **0**, **leave page in memory**, and replace **next page**, subject to **same rules**.

Second-Chance Algorithm (2/2)



Counting Page Replacement



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- ▶ Keep a **counter** of the **number of references** that have been made to each page.



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- ▶ **Least Frequently Used (LFU)** algorithm: replaces page with **smallest count**.
- ▶ **Most Frequently Used (MFU)** algorithm: based on the argument that the page with the smallest count was **probably just brought in** and has yet to be used.

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- ▶ Partially-loaded programs
- ▶ Virtual memory: much larger than physical memory
- ▶ Demand paging similar to paging + swapping
- ▶ Page fault
- ▶ Page replacement algorithms:
 - FIFO, optimal, LRU, LRU-approximate, counting-based

Questions?

Acknowledgements

Some slides were derived from Avi Silberschatz slides.